

INTERNATIONAL AS MATHEMATICS

MA01

(9660/MA01) Unit P1 Pure Mathematics

Mark scheme

January 2024

Version: 1.0 Final



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Key to mark scheme abbreviations

M	Mark is for method
m	Mark is dependent on one or more M marks and is for method
A	Mark is dependent on M or m marks and is for accuracy
B	Mark is independent of M or m marks and is for method and accuracy
E	Mark is for explanation
✓ or ft	Follow through from previous incorrect result
CAO	Correct answer only
CSO	Correct solution only
AWFW	Anything which falls within
AWRT	Anything which rounds to
ACF	Any correct form
AG	Answer given
SC	Special case
oe	Or equivalent
A2, 1	2 or 1 (or 0) accuracy marks
–x EE	Deduct x marks for each error
NMS	No method shown
PI	Possibly implied
SCA	Substantially correct approach
sf	Significant figure(s)
dp	Decimal place(s)
ISW	Ignore subsequent working

Q	Answer	Marks	Comments
1(a)(i)	$-\frac{7}{2}$	B1	
		1	

Q	Answer	Marks	Comments
1(a)(ii)	$-\frac{33}{2}$	B1	
		1	

Q	Answer	Marks	Comments
1(b)	<p>Correctly orientated symmetrical parabola</p> <p>$(0,8)$ labelled on the y-axis</p> <p>Vertex labelled as $\left(\frac{7}{2}, -\frac{33}{2}\right)$</p>	<p>B1</p> <p>B1</p> <p>B1ft</p>	<p>Condone label given as y-value only.</p> <p>ft Their $(-a,b)$ from part (a)</p> <p>Accept correctly positioned vertex with $x = \frac{7}{2}$ and $y = -\frac{33}{2}$ indicated on axes.</p>
		3	
	Question 1 Total	5	

Q	Answer	Marks	Comments
2(a)	$[y = 0 \Rightarrow 3x + 2 \times 0 - 66 = 0 \Rightarrow x = 22]$ $(22, 0)$	B1	Correct coordinates of P Condone only correct x -coordinate given.
		1	

Q	Answer	Marks	Comments
2(b)	$[\text{Gradient of } l_1 =] -\frac{3}{2}$ $[y = 0 \Rightarrow 0 = -\frac{3}{2}x - 6 \Rightarrow x = -4]$ $(-4, 0)$	M1 A1	oe Correct gradient of l_1 Correct coordinates of Q Condone only correct x -coordinate given.
		2	

Q	Answer	Marks	Comments
2(c)(i)	$\left[-\frac{3}{2} \times m_{QR} = -1 \Rightarrow \right]$ $\left[m_{QR} = \right] \frac{2}{3}$ $y - 0 = \frac{2}{3}(x - (-4)) \text{ or } y = \frac{2}{3}x + \frac{8}{3}$ $(14, 12)$	<p>B1</p> <p>M1</p> <p>A2,1</p>	<p>PI Correct gradient of QR ft Their gradient of l_1 and/or l_2 from part (b) Forms equation of QR ft Their gradient of QR and coordinates of Q ACF</p> <p>Solves $3x + 2y - 66 = 0$ and $y = \frac{2}{3}x + \frac{8}{3}$ simultaneously. Accept $x = 14$ and $y = 12$ but must be clearly identified A1: One correct coordinate A2: Correct coordinates</p>
		4	

Q	Answer	Marks	Comments
2(c)(ii)	$\frac{1}{2} \times (22 - (-4)) \times 12$ $= 156$	<p>M1</p> <p>A1</p>	<p>ft their coordinates of P, Q and R provided P and Q are of the form $(x, 0)$ oe May see $\frac{1}{2} \times PR \times QR = \frac{1}{2} \times 4\sqrt{13} \times 6\sqrt{13}$ CAO</p>
		2	

	Question 2 Total	9	
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[illegible]

Q	Answer	Marks	Comments
3(b)	$10t^2 + 27t - 28 = w\sqrt{5t} - 2w$ or $10t^2 + 27t - 28 = w(\sqrt{5t} - 2)$ $[w=] \frac{(10t^2 + 27t - 28)(\sqrt{5t} + 2)}{(\sqrt{5t} - 2)(\sqrt{5t} + 2)}$ $[w=] \frac{(5t - 4)(2t + 7)(\sqrt{5t} + 2)}{5t - 4}$ $[w=] (2t + 7)(\sqrt{5t} + 2)$	M1 M1 M1 A1	<p>oe Isolates terms in w on one side. Condone one error.</p> <p>oe Divides both sides by $\sqrt{5t} - 2$ and multiplies numerator and denominator by $\sqrt{5t} + 2$ Denominator may be simplified or unsimplified.</p> <p>Factorises $10t^2 + 27t - 28$ correctly in their expression. Accept denominator not expanded. PI by correct final answer but M1M1 must have been awarded.</p> <p>Must be convincingly shown. CAO</p>
3(b) ALT	$10t^2 + 27t - 28 = w\sqrt{5t} - 2w$ or $10t^2 + 27t - 28 = w(\sqrt{5t} - 2)$ $(5t - 4)(2t + 7) = w(\sqrt{5t} - 2)$ $(\sqrt{5t} - 2)(\sqrt{5t} + 2)(2t + 7) = w(\sqrt{5t} - 2)$ or $[w=] \frac{(\sqrt{5t} - 2)(\sqrt{5t} + 2)(2t + 7)}{(\sqrt{5t} - 2)}$ $[w=] (2t + 7)(\sqrt{5t} + 2)$	M1 M1 M1 A1	<p>oe Isolates terms in w on one side.</p> <p>oe Factorises LHS correctly in their equation.</p> <p>oe Factorises $(5t - 4)$ PI by correct final answer but M1M1 must have been awarded.</p> <p>Must be convincingly shown. CAO</p>
		4	

	Question 3 Total	7	
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Q	Answer	Marks	Comments
5(a)	$\frac{1}{6}d \times \left(-\frac{1}{4}d\right) \times \left(-\frac{1}{4}d\right) = 18$ $\frac{1}{96}d^3 = 18 \text{ or}$ $d^3 = 1728 \text{ or } d = \sqrt[3]{1728}$ and $d = 12$	M1 A1	<p>oe Uses x-coordinates of x-intercepts with or without signs completely reversed, and set equal to 18</p> <p>PI by $\frac{1}{96}d^3 = 18 \text{ or}$ $d^3 = 1728 \text{ or } d = \sqrt[3]{1728}$</p> <p>oe</p> <p>AG</p>
		2	

[illegible]

Q	Answer	Marks	Comments
6(a)	$\frac{x}{8} = \frac{6}{y}$ or $\frac{x+6}{y+8} = \frac{x}{8}$ or $\frac{x+6}{y+8} = \frac{6}{y}$ or $xy = 48$ or $[y =] \frac{48}{x}$ or $\frac{x}{6} = \frac{8}{y}$ $[T =] 48 + 4x + 3y$ or $[T =] \frac{1}{2}(x+6)(y+8)$ or $[T =] \frac{1}{2}(xy + 8x + 6y + 48)$ or $[T =] \frac{1}{2}xy + 4x + 3y + 24$ $48 + 4x + 3 \times \frac{48}{x}$ or $24 + \frac{144}{x} + 4x + 24$ or $[T =] \frac{1}{2} \left(48 + 8x + 6 \times \frac{48}{x} + 48 \right)$ or $[T =] \frac{1}{2} \times 48 + 4x + 3 \times \frac{48}{x} + 24$ and $T = 48 + 4x + \frac{144}{x}$	<p>B1</p> <p>M1</p> <p>A1</p>	<p>oe Finds relationship between x and y</p> <p>oe Forms an expression for the area of the triangle.</p> <p>oe Extra line of working with 'y's eliminated and AG Be convinced.</p>
		3	

Q	Answer	Marks	Comments
6(b)(i)	$\left[\frac{dT}{dx} = \right] 4 - \frac{144}{x^2}$ $4 - \frac{144}{x^2} = 0$ $[x =] 6$ $\left[x = 6 \Rightarrow T = 48 + 4 \times 6 + \frac{144}{6} = \right] 96$	<p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p>	<p>oe Correct derivative</p> <p>Sets their derivative to equal zero</p> <p>CAO Ignore $x = -6$ if seen</p> <p>CAO</p>
		4	

Q	Answer	Marks	Comments
6(b)(ii)	$\left[\frac{d^2T}{dx^2} = \right] \frac{288}{x^3}$ $\left[x = 6 \Rightarrow \frac{d^2T}{dx^2} = \right] \frac{288}{6^3} \left[= \frac{288}{216} = \frac{4}{3} \right]$ <p>and since $\frac{d^2T}{dx^2} > 0$ it is a minimum value of T</p>	<p>B1ft</p> <p>E1ft</p>	<p>oe ft their first derivative from part (b)(i) and second derivative must be of the form $\frac{k}{x^3}$ where $k > 0$ $x = 6$ substituted into their second derivative and concluding statement made. ft their value of x provided it is positive Second derivative must be of the form $\frac{a}{x^3}$ oe.</p>
		2	

	Question 6 Total	9	
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Q	Answer	Marks	Comments
7(a)	$\left[\frac{dy}{dx} = \right] 4 - \frac{1}{2}x$	B1	Correct derivative
	$\left[x = 4 \Rightarrow \frac{dy}{dx} = \right] 2$	B1	Correct gradient of l
	$y - 24 = 2(x - 5)$ or $[y =]2x + 14$	M1	ACF Forms a correct equation for l
	$35 + 4x - \frac{1}{4}x^2 = 2x + 14$	M1	ft Their expression for y in terms of x oe Eliminates y
	$\frac{1}{4}x^2 - 2x - 21 = 0$ and $x^2 - 8x - 84 = 0$	A1	oe Must see a second line of working before AG
		5	

Q	Answer	Marks	Comments
7(b)	$[x =] -6$ and $[x =] 14$	B1	Correct critical values
	$-6 < x < 14$	B1	CAO Accept interval notation $(6,14)$ but not $[6,14]$.
		2	

Q	Answer	Marks	Comments
7(c)(ii) ALT	$\int_{-6}^{14} \left(35 + 4x - \frac{1}{4}x^2 \right) - (2x + 14) dx$	M1	Sets up a single integral PI by correct final answer.
	$\int_{-6}^{14} \left(21 + 2x - \frac{1}{4}x^2 \right) dx$		
	$\left[21x + x^2 - \frac{1}{12}x^3 \right]_{-6}^{14}$	M1	Correct integration at least two terms correct.
		A1	All correct. PI
	$[F(14) - F(-6)] = \frac{784}{3} - (-72)$	M1	Correct substitution. Simplified or unsimplified. PI
	$\frac{1000}{3} \text{ or } 333\frac{1}{3}$	A1	Correct value for required area If given as decimal AWRT 333.33 NMS scores zero.
		5	

	Question 7 Total	14	
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Q	Answer	Marks	Comments
8(a)	$\left[(1-w)^3\right] = 1-3w+3w^2-w^3$	B1	
		1	

Q	Answer	Marks	Comments
8(b)	$\left[(1-\sqrt{x})^3 = \right] 1-3\sqrt{x}+3(\sqrt{x})^2-(\sqrt{x})^3$ $=1-3\sqrt{x}+3x-x\sqrt{x}$ <p>or</p> $\left[(1+\sqrt{x})^3 = \right] 1-3(-\sqrt{x})+3(-\sqrt{x})^2-(-\sqrt{x})^3$ $=1+3\sqrt{x}+3x+x\sqrt{x}$ $4(1-3\sqrt{x}+3x-x\sqrt{x})+1+3\sqrt{x}+3x+x\sqrt{x}$ <p>or</p> $4-12\sqrt{x}+12x-4x\sqrt{x}+1+3\sqrt{x}+3x+x\sqrt{x}$ $5-9\sqrt{x}+15x-3x\sqrt{x}$	<p>B1ft</p> <p>M1</p> <p>A2,1</p>	<p>ft their answer to part (a)</p> <p>PI oe Correct expansion of $(1-\sqrt{x})^3$ or $(1+\sqrt{x})^3$ or $(1+w)^3$ simplified or unsimplified.</p> <p>PI oe Substitutes their expansions into $4(1-\sqrt{x})^3+(1+\sqrt{x})^3$</p> <p>Must be expression in the correct form. A1 for a or b correct. A2 for a and b both correct.</p>
		4	

Q	Answer	Marks	Comments
8(c)	$5 - 9x^{\frac{1}{2}} + 15x - 3x^{\frac{3}{2}}$ $\left[\int \left(5 - 9x^{\frac{1}{2}} + 15x - 3x^{\frac{3}{2}} \right) dx = \right]$ $5x - \frac{2}{3} \times 9x^{\frac{3}{2}} + \frac{15}{2} x^2 - \frac{2}{5} \times 3x^{\frac{5}{2}} [+c]$ or $5x - 6x^{\frac{3}{2}} + \frac{15}{2} x^2 - \frac{6}{5} x^{\frac{5}{2}} [+c]$ $5 \times 4 - 6 \times 4^{\frac{3}{2}} + \frac{15}{2} \times 4^2 - \frac{6}{5} \times 4^{\frac{5}{2}} + c = 20$ or $20 - 48 + 120 - \frac{192}{5} + c = 20$ $y = 5x - 6x^{\frac{3}{2}} + \frac{15}{2} x^2 - \frac{6}{5} x^{\frac{5}{2}} - \frac{168}{5}$	<p>B1ft</p> <p>M1 A1ft</p> <p>M1</p> <p>A1</p>	<p>PI ft their answer to part (b) Correctly rewrites integrand as powers of x</p> <p>ft their integrand. M1: At least one term with fractional power correctly integrated, simplified or unsimplified. A1ft: Fully correct integration with simplified coefficients using their integrand.</p> <p>oe Substitutes $x = 4$ into their integral and sets it equal to 20 Must have '$+c$' at this stage.</p> <p>PI by $c = -\frac{168}{5}$ or $c = -33.6$</p> <p>ACF With simplified coefficients.</p>
		5	

	Question 8 Total	10	
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Q	Answer	Marks	Comments
9(a)	$\left[\frac{u_2}{u_1} = \frac{u_3}{u_2} \Rightarrow \right] \frac{b}{a} = \frac{c}{b}$ $\left[b^2 = ac \Rightarrow (27c^2)^2 = ac \Rightarrow c^4 = \frac{ac}{729} \Rightarrow \right]$ $\left[c^3 = \right] \frac{a}{729} \text{ or } \left[c = \right] \frac{a^{\frac{1}{3}}}{9}$ or $729c^3 = a$ or $9c = a^{\frac{1}{3}}$ $\left[b^2 = ac \Rightarrow b^2 = \right] \frac{a^{\frac{4}{3}}}{9}$ $\left[b = \right] \frac{a^{\frac{2}{3}}}{3}$	<p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p>	<p>PI oe Forms a correct equation relating a, b and c</p> <p>oe Uses $b^2 = ac$ to form an expression for c^3 or c or an equation in terms of a and c</p> <p>oe Simplified or unsimplified. Uses $b^2 = ac$ and eliminates c PI by correct unsimplified final answer.</p> <p>oe Must be simplified Allow $u_2 = \frac{a^{\frac{2}{3}}}{3}$ and $u_2 = \frac{\sqrt[3]{a^2}}{3}$</p>
		4	

Q	Answer	Marks	Comments
9(a) ALT	$\left[\frac{u_2}{u_1} = \frac{u_3}{u_2} \Rightarrow \right] \frac{b}{a} = \frac{c}{b}$	M1	PI oe Forms a correct equation relating a , b and c
	$\left[b^2 = ac \Rightarrow c = \frac{b^2}{a} \Rightarrow \right]$ $b = 27 \left(\frac{b^2}{a} \right)^2 \quad \text{or} \quad b = \frac{27b^4}{a^2}$	M1	PI oe Uses $b^2 = ac$ to eliminate c in $b = 27c^2$
	$[b^3 =] \frac{a^2}{27}$	M1	oe Correct expression for b^3 in terms of a PI by correct unsimplified final answer.
	$[b =] \frac{a^{\frac{2}{3}}}{3}$	A1	oe Must be simplified. Allow $u_2 = \frac{a^{\frac{2}{3}}}{3}$ and $u_2 = \frac{\sqrt[3]{a^2}}{3}$
		4	

