

Please write clearly in block capitals.

Centre number 

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Candidate number 

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Surname \_\_\_\_\_

Forename(s) \_\_\_\_\_

Candidate signature \_\_\_\_\_

I declare this is my own work.

# INTERNATIONAL A-LEVEL FURTHER MATHEMATICS

(9665/FM04) Unit FS2 Statistics

Wednesday 22 January 2020 07:00 GMT Time allowed: 1 hour 30 minutes

## Materials

- For this paper you must have the Oxford International AQA booklet of formulae and statistical tables (enclosed).
- You may use a graphics calculator.

## Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

## Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.

## Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- Show all necessary working; otherwise marks may be lost.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
9	
<b>TOTAL</b>	



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ANSWER IN THE SPACES PROVIDED**



**1** Fiona is tossing an unbiased coin with 'heads' on one side and 'tails' on the other.

She is playing a game where she gets 10 points if the coin lands with 'heads' facing up and 0 points if it lands with 'tails' facing up.

She tosses the coin twice.

**[3 marks]**

[illegible]

Answer

3



Andrew estimates the mean by taking a random sample,  $X_1$ , of size 10 from  $X$  and calculating the sample mean  $\overline{X_1}$

$X_1$  and  $X_2$  are independent.

Both  $\overline{X}_1$  and  $\overline{X}_2$  are unbiased estimators of  $\mu$ .

Interpret your answer.

**[3 marks]**

[illegible]

2 (b) (i) Show that  $P = \frac{\overline{X_1} + \overline{X_2}}{2}$  is an unbiased estimator of  $\mu$ .

[2 marks]

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2 (b) (ii) Find  $\text{Var}(P)$ .

[2 marks]

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Answer \_\_\_\_\_

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Turn over ►



He takes a random sample of 500 people. The results are

**3 (a)** Abdul assumes that age at retirement is a normal distribution.

**[6 marks]**

[illegible]

Answer



- 3 (b)** Abdul uses his random sample to conduct a hypothesis test at the 4% level of significance with hypotheses

$$H_0: \mu = 67$$

$$H_1: \mu \neq 67$$

Using the confidence interval found in part (a), explain whether Abdul accepts or rejects the null hypothesis.

**[1 mark]**

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- 3 (c)** After further investigation, Abdul concludes that age at retirement is not a normal distribution.

Explain whether or not the confidence interval found in part (a) is still valid.

**[2 marks]**

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**4 (a) (ii)** Find the power of the test, giving your answer to three significant figures.

**[2 marks]**

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Answer \_\_\_\_\_

**4 (b)** State how increasing the level of significance for the hypothesis test will affect the power of the test.

**[1 mark]**

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7
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**Turn over for the next question**

**Turn over ►**



The length of fabric produced per minute by machine  $A$  and the length of fabric produced per minute by machine  $B$  both have normal distributions which are independent of each other.

The company takes a random sample of 21 lengths of fabric, each produced in a minute, from machine  $A$ .

The sample standard deviation for machine  $A$  is 0.3 metres.

Test the company's claim that the population variances for the two machines are equal, using the 2% level of significance.

[illegible]

[illegible]

**7**

A company performed a survey of its employees in both its northern offices and its southern offices about the transport that the employees use to get to work.

	Walk	Car	Bus	Train	Total
Northern	4	32	30	2	68
Southern	22	15	20	5	62
Total	26	47	50	7	130

**[10 marks]**

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outside the  
box

Handwriting practice area with 25 horizontal lines.

Turn over ►



The supermarket claims that the mean mass of jars of honey is different for the two suppliers.

**[7 marks]**

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- 7 (b) Explain what changes would need to be made to the test carried out in part (a) if only sample standard deviations were available and assuming that the population standard deviations were equal.

[4 marks]



Student	Before	After
1	20	24
2	18	19
3	16	16
4	10	9
5	5	7
6	3	6

**8 (a)** Test the tutorial company's claim, using the 5% level of significance.

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**[2 marks]**

[illegible]

13

- 9 The random variable  $X$  has moment generating function  $M_X(t)$  where

$$M_X(t) = 0.04(1 - 0.8e^t)^{-2}$$

- 9 (a) Find the mean of  $X$ .

[4 marks]

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Answer \_\_\_\_\_

- 9 (b) Find the variance of  $X$ .

[4 marks]

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Answer \_\_\_\_\_



**[3 marks]**

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Answer

**Question 9 continues on the next page**

**Turn over ►**



**9 (d)**

$$M_Y(t) = (0.8 + 0.2e^t)^2$$

$X$  and  $Y$  are independent.

Find  $M_{X+Y}(t)$ , giving your answer in the form  $\left(\frac{a+be^t}{1-0.8e^t}\right)^2$ , where  $a$  and  $b$  are constants.

**[2 marks]**

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Answer

13

**END OF QUESTIONS**



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[illegible]

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