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# INTERNATIONAL AS FURTHER MATHEMATICS

(9665/FM02) Pure Maths, Statistics and Mechanics Unit FPSM1

Thursday 24 January 2019 07:00 GMT Time allowed: 1 hour 30 minutes

## Materials

- For this paper you must have the Oxford International AQA booklet of formulae and statistical tables.
- You may use a graphics calculator.

## Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the boxes at the top of this page.
- Answer all questions.
- You must answer the questions in the spaces provided. Do not write outside the box on each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

## Information

- The marks for questions are shown in brackets.
- There are three sections to this paper.
- The maximum mark for this paper is 80. There are 40 marks for **Section A**, 20 marks for **Section B** and 20 marks for **Section C**.

## Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- Show all necessary working; otherwise marks may be lost.



For Exam	iner's Use
Question	Mark
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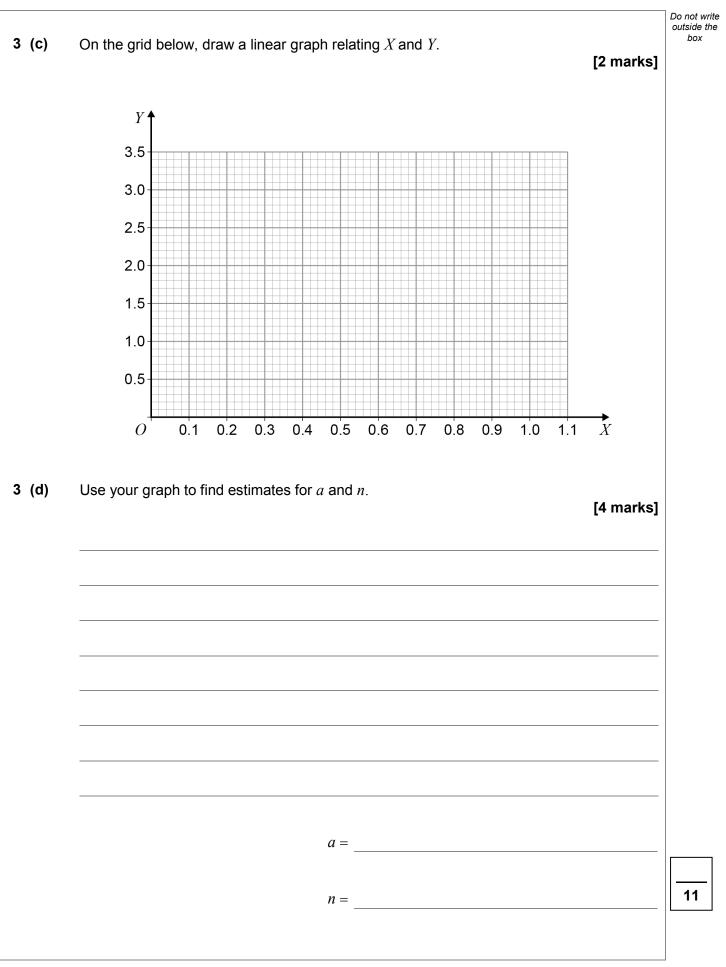
Section A	
Answer <b>all</b> questions in the spa	aces provided.
A curve passes through the point (1.2, 0.8) and	satisfies the differential equation
$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{1}{x^2}$	$\frac{1}{+y^2}$
Use Euler's step-by-step method with a step ler of $y$ when $x = 1.4$	ngth of 0.1 to estimate the value
Give your answer to three decimal places.	
	[5 marks]
Answer	



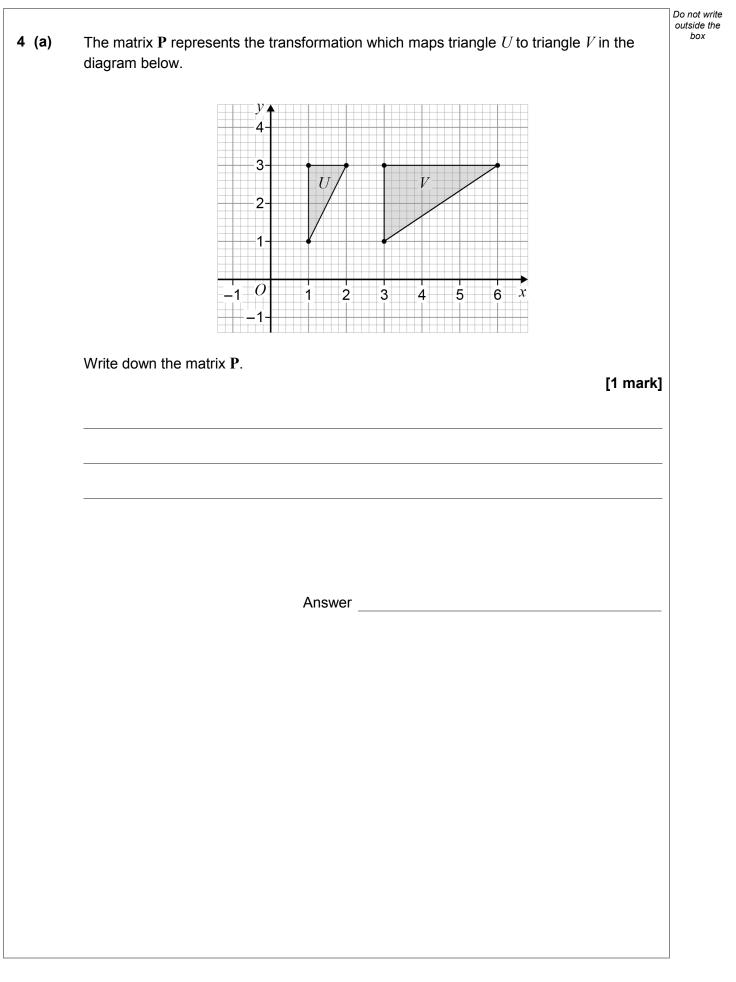
2	The equation	Do not write outside the box
-	$x^3 - 8x - 12 = 0$	
	has a real root, $\alpha$ , in the interval 3 < x < 4	
	Use linear interpolation to show that $\alpha$ is in the interval $\frac{96}{29} < x < 4$ [5 marks]	
	Turn over for the next question	5
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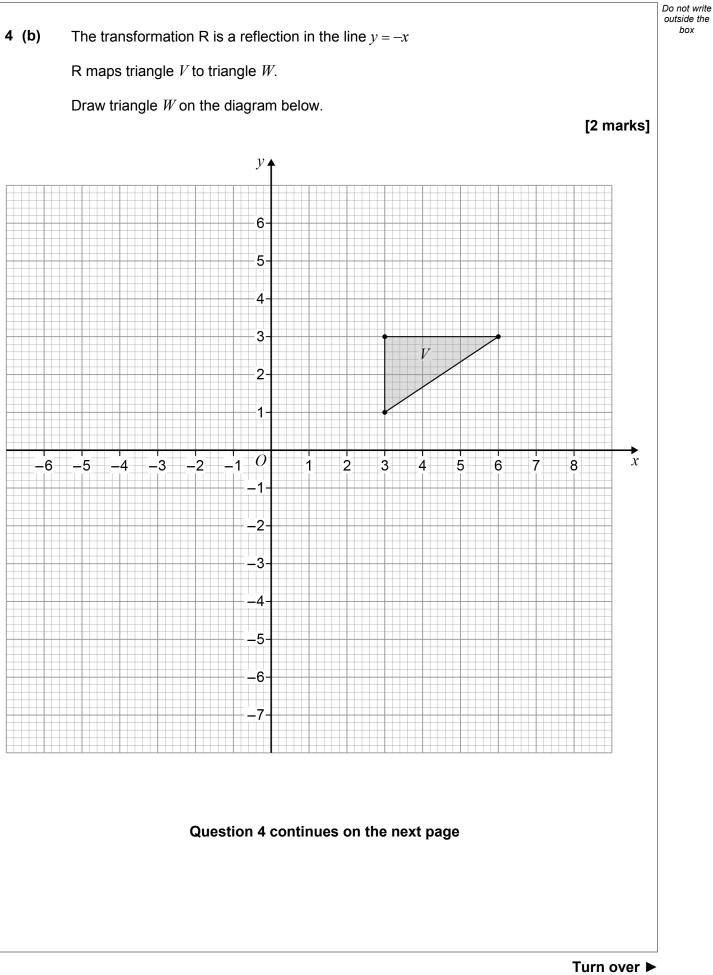




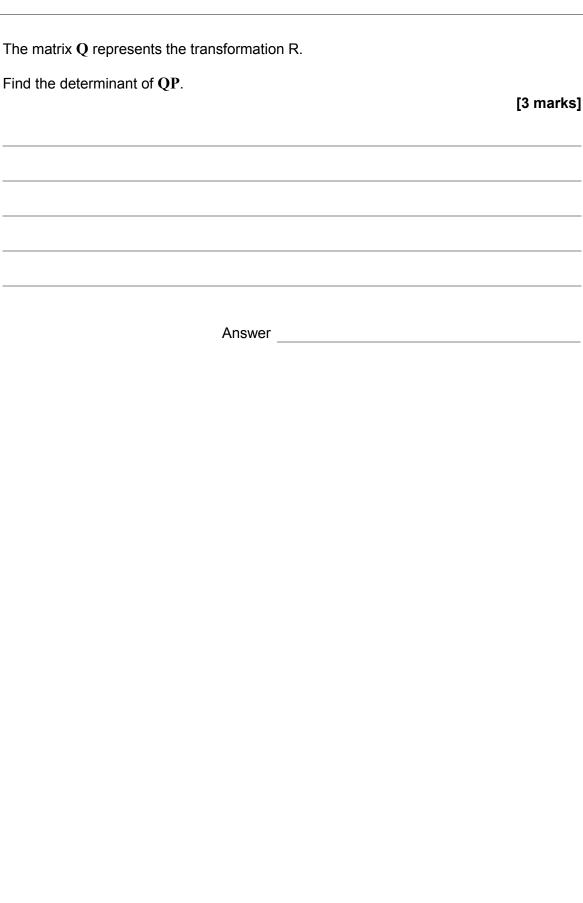








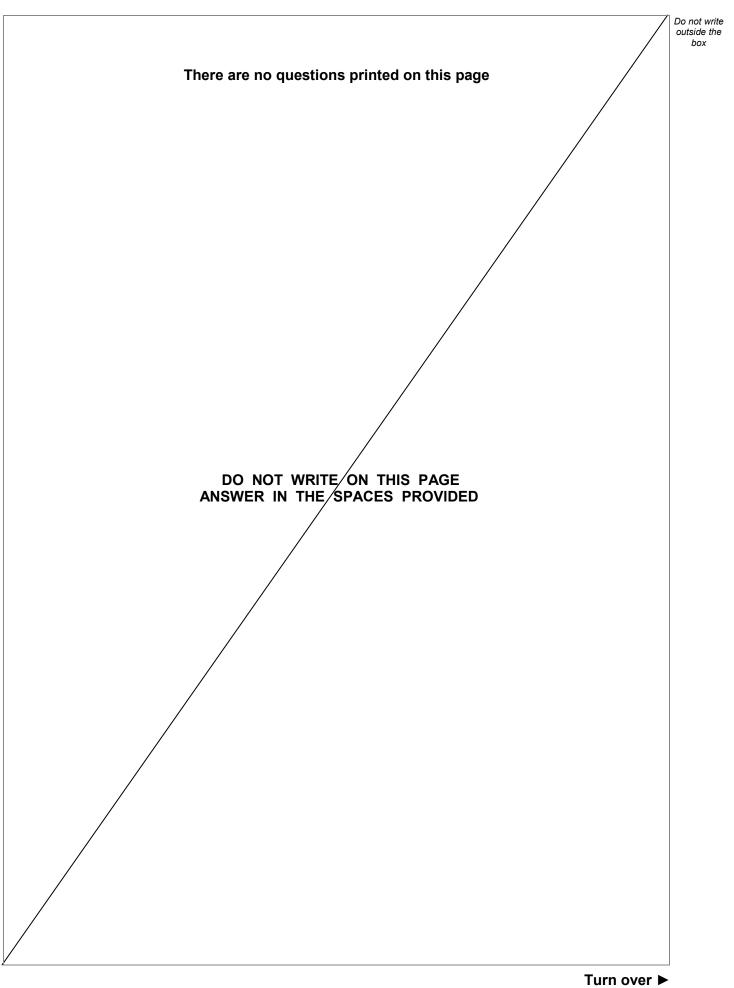






4 (c)

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5	The matrix <b>B</b> is defined by $\mathbf{B} = \begin{bmatrix} -1 & 1 \\ -1 & -1 \end{bmatrix}$ The matrix <b>C</b> is defined by $\mathbf{C} = \begin{bmatrix} 2 & 4 \\ 2 & 6 \end{bmatrix}$ The matrix <b>A</b> is such that $\mathbf{AB} = \mathbf{C}$ .	Do not write outside the box
5 (a)	Find A. [4 marks]	
	Answer	

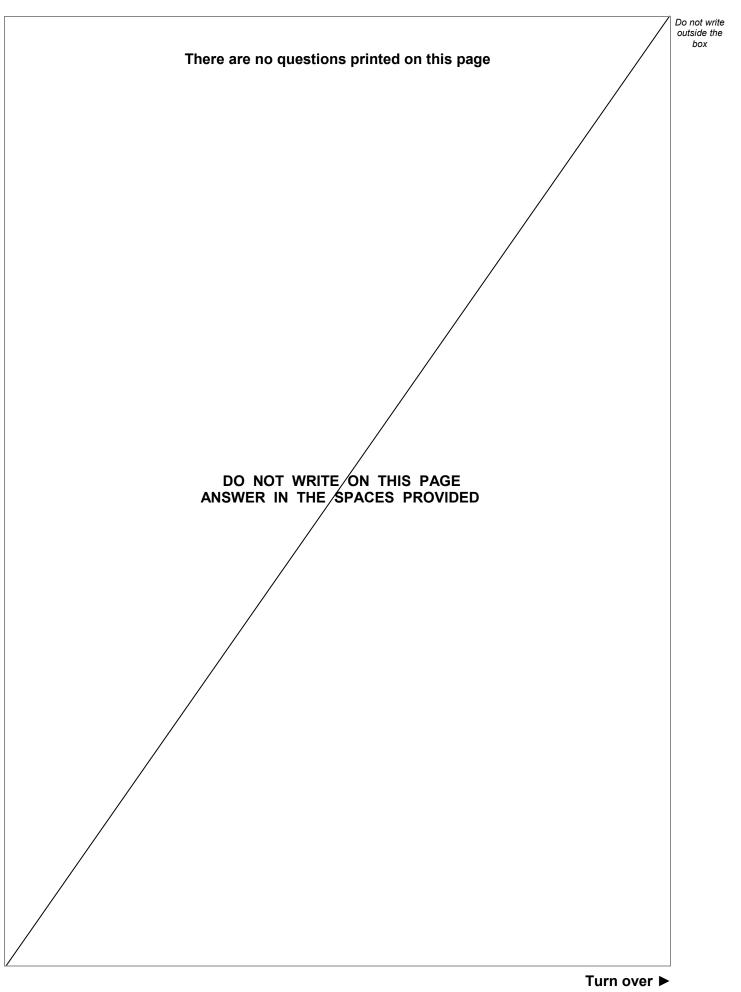


5	(b)		Show that <b>B</b> <sup>4</sup> = <i>k</i> <b>I</b> for some integer <i>k</i> , where <b>I</b> is the 2 × 2 identity matrix.	[4 marks]	Do not write outside the box
5	(c)		The matrix ${f B}$ represents a combination of an enlargement and a rotation.		
5	(c)	(i)	Find the scale factor of the enlargement.	[1 mark]	
			Answer		
5	(c)	(ii)	Find the angle of the rotation.	[1 mark]	
			Answer		



5 (d)	Use your answer to part (b) to find $B^{21}$ [3 marks]	Do not write outside the box
	Answer	
		13







	Section B	IDo not write outside the box
	Answer <b>all</b> questions in the spaces provided.	
6	X is a discrete uniform distribution where $x$ can take the value 1, 2 or 3	-
6 (a)	Find P(X > 1) [1 mark]	
	Answer	
6 (b)	Derive the probability generating function, $G_X(t)$ , of X. [2 marks]	
	Answer	

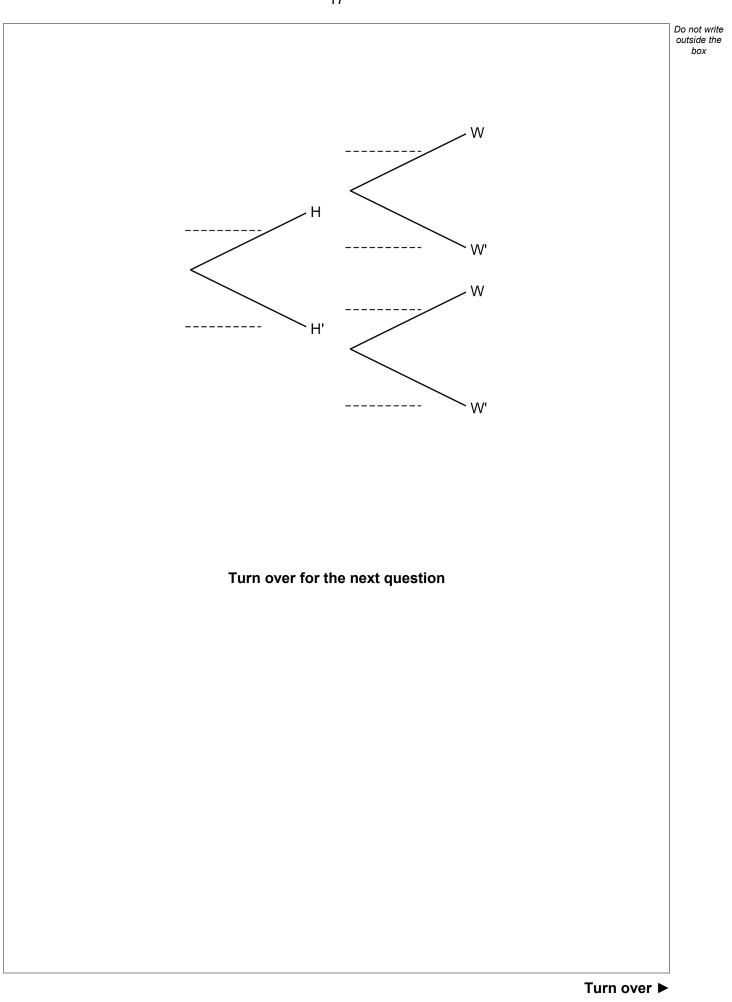


Given that X and Y are independent, find P(X + Y = 1)       [3 marks]	6 (c)	Y is a discrete random variable with probability generating function $G_{Y}(t)$ where	Do not write outside the box
[3 marks]			
		Given that X and Y are independent, find $P(X + Y = 1)$ [3 marks]	
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7	To prepare for a tennis tournament, Holly plays practice tennis matches until she wins a match.	Do not write outside the box
	The results of different tennis matches are independent.	
	The probability that Holly wins a practice tennis match is 0.6	
	Let $H$ represent the event that Holly plays more than 3 practice tennis matches.	
7 (a)	Find P( <i>H</i> ). [1 mark]	
	Answer	
7 (b)	Let $W$ represent the event that Holly wins the tennis tournament.	
	Given that $P(W) = 0.7$ and $P(H W) = 0.01$ , complete the tree diagram opposite by finding the probability for each branch. [5 marks]	
		<b></b>
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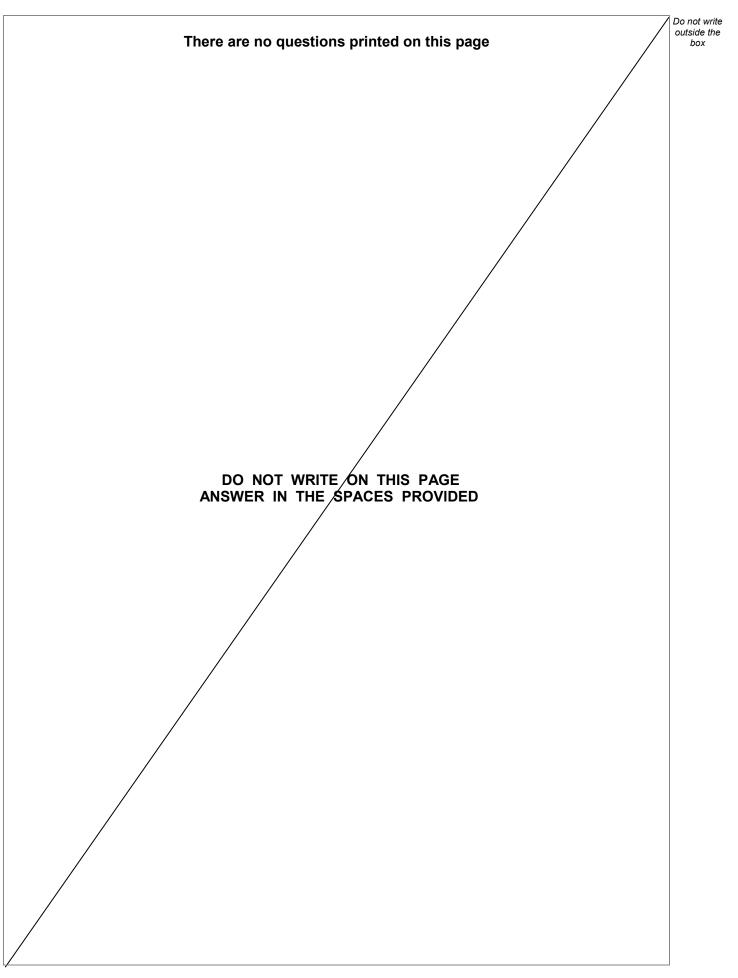


		Do not write outside the
8	The discrete random variable $P$ has:	box
	E(P) = 2	
	$E(P^2) = 5$	
	$E(P^3) = 14.6$	
	The discrete random variable $Q$ is such that $Q = 2P^2 - 5$	
8 (a)	Find Cov( <i>P</i> , <i>Q</i> ). [5 marks]	
	Answer	



8 (b)	The variance of $Q$ is 8	Do not write outside the box
	Find $Var(P + Q)$ . [3 marks]	
	Answer	
	Turn over for the next question	8
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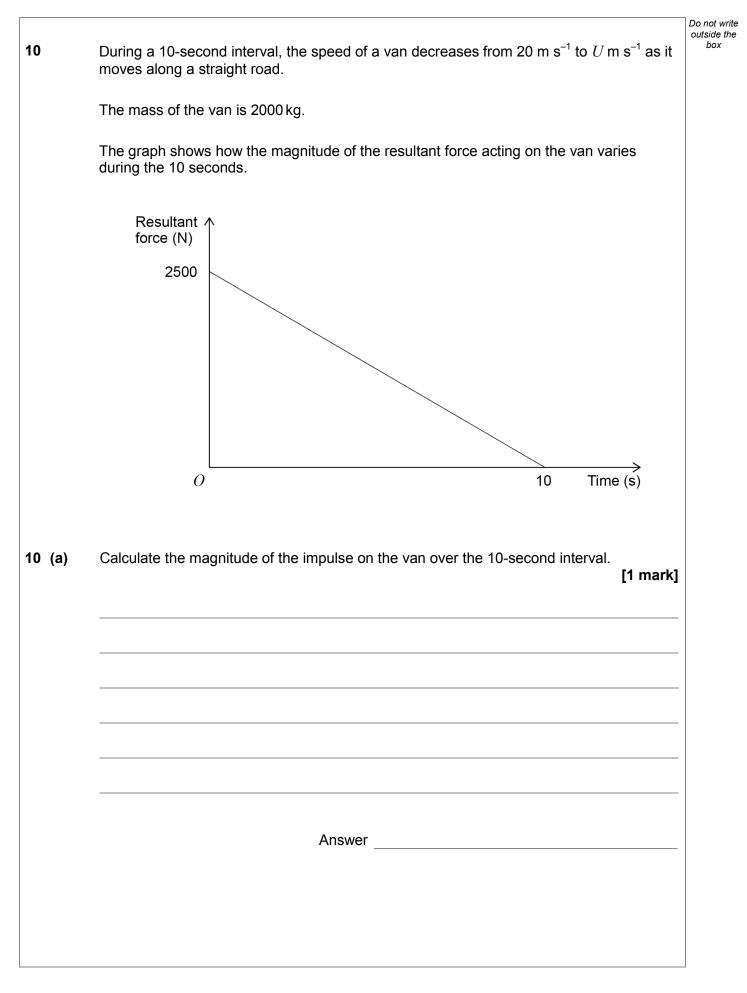




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	Section C	Do not write outside the box
	Answer <b>all</b> questions in the spaces provided.	
9	A model for the resistance force, <i>R</i> newtons, acting on a sphere moving with speed $v \text{ m s}^{-1}$ through a fluid is given by $R = k v^{\frac{3}{2}}$	
	where $k$ is a constant.	
	Find the dimensions of $k$ in terms of M, L and T. [2 marks]	
	Answer	
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	Turn over for the next question	
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10 (b)	Find U.	Do not write outside the box
	[3 marks]	
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		Do not write outside the
11	Two discs, <i>A</i> and <i>B</i> , are the same size.	box
	Disc A has mass m and disc B has mass 4m.	
	The discs are moving in the same direction along a straight line on a smooth horizontal surface when they collide.	
	Just before the collision, disc $A$ has speed 5 $U$ and disc $B$ has speed $U$ .	
	The coefficient of restitution between the two discs is <i>e</i> .	
11 (a)	Find the speed of <i>B</i> after the collision, giving your answer in terms of $e$ and $U$ . [5 marks]	
	Answer	



11 (b)	After the collision, A moves in the opposite direction.	Do not write outside the box
	Find an inequality that <i>e</i> must satisfy. [3 marks]	
	[· · · · · · · · · · · · · · · · · · ·	
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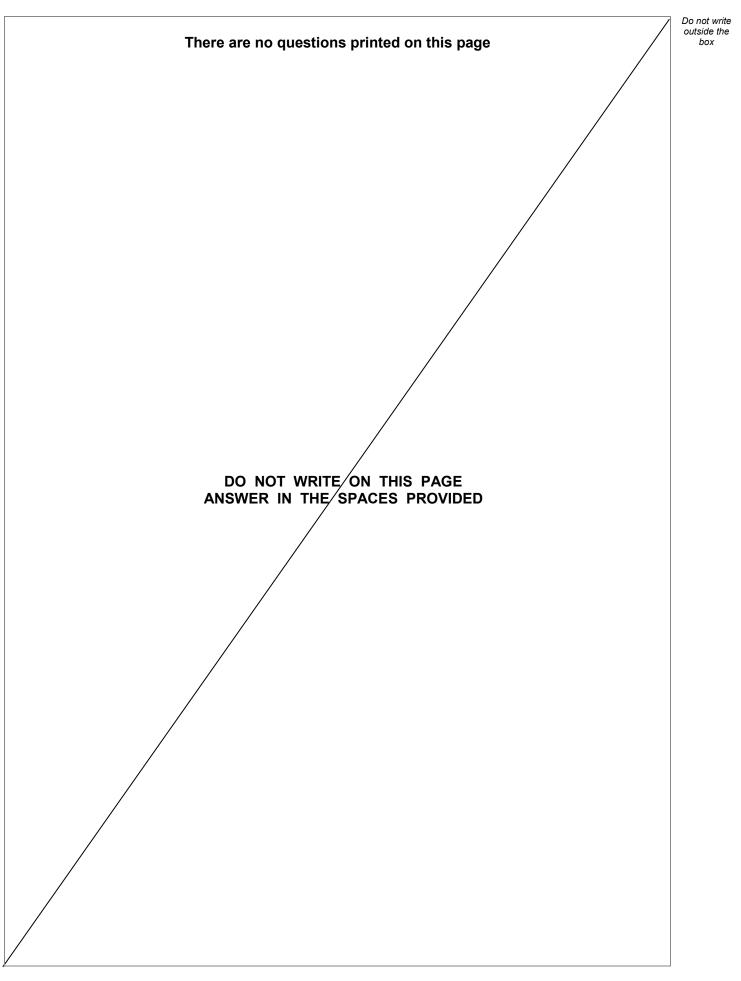
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Do not write outside the box A boat is moving with a constant velocity of 8 m  $s^{-1}$  on a bearing of 030° 12 A ship is moving north with a constant velocity of 5 m  $\rm s^{-1}$ Initially the ship is 2000 metres east of the boat. The diagram shows the initial positions and the velocities of the boat and the ship. Ν 8 m s<sup>-1</sup> 30° 5 m s<sup>-1</sup> Boat 2000 m Ship Find the minimum distance between the boat and the ship giving your answer to 3 significant figures. [6 marks]



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END OF QUESTIONS	







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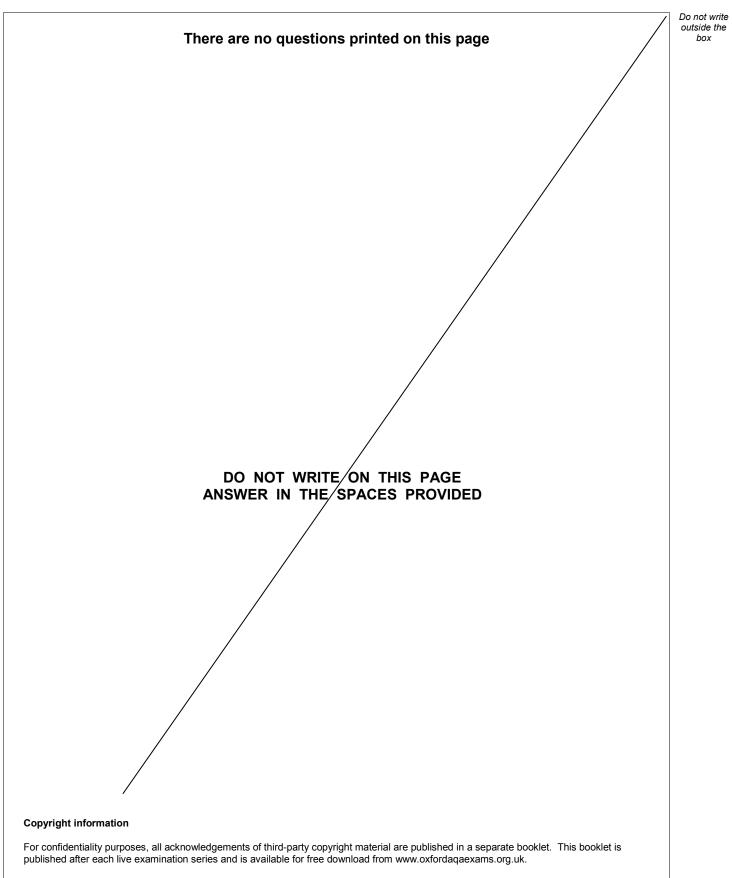


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