

Please write clearly in block capitals.

Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

INTERNATIONAL AS FURTHER MATHEMATICS

Further Pure Mathematics Unit 1

Thursday 31 May 2018

07:00 GMT

Time allowed: 1 hour 30 minutes

Materials

- For this paper you must have the booklet of formulae and statistical tables, which is included as an insert.
- You may use a graphics calculator.

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Fill in the box at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box on each page or on blank pages. If you require extra space, use a supplementary answer book.
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.

Advice

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.
- Show all necessary working; otherwise marks may be lost.

For Examiner's Use	
Question	Mark
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	
TOTAL	



Answer **all** questions in the spaces provided.

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outside the
box

1 A curve has the equation $y = 2x^2 - 4x$

1 (a) A line passes through two points on the curve, one where $x = 3$ and the other where $x = 3 + h$

Find the gradient of this line in the form $p + qh$, where p and q are integers.

[3 marks]

Answer _____

1 (b) Show how the answer to part **(a)** can be used to find the gradient of the curve at the point where $x = 3$

State the value of this gradient.

[2 marks]

Answer _____

5



Also, $\frac{3-2i}{z} = a + ib$, where a and b are real.

[3 marks]

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Answer

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3

Turn over ►



$$f(r) - f(r+1) = \frac{1}{(r+2)(r+3)}$$

3 (b) (i) find the exact value of

$$\sum_{r=11}^{30} \frac{1}{(r+2)(r+3)}$$

[illegible]

Answer



3 (b) (ii) show that

$$\sum_{r=18}^{\infty} \frac{1}{(r+2)(r+3)} = \frac{1}{m}$$

where m is an integer.

[4 marks]

9

Turn over for the next question

Turn over ►



- 4 Find the general solution of the equation

$$\cos\left(3x + \frac{\pi}{6}\right) = \frac{1}{\sqrt{2}}$$

giving your answer in terms of π .

[5 marks]

Answer _____

5



[The volume V of a cone is given by the formula $V = \frac{1}{3}\pi r^2 h$, where r is the radius of the circular base of the cone and h is the height of the cone.]

The diagram shows a large inverted triangle with a horizontal top base of 6 m. A vertical line segment from the top base to the bottom vertex represents the height, which is labeled as 4 m on the right side. Inside this large triangle, there is a smaller, shaded inverted triangle. The height of this shaded triangle, measured from its top base to its bottom vertex, is labeled as h m.

[8 marks]

[illegible]

6 (a) Find the value of

$$\sum_{r=1}^{45} (2r)^2$$

[2 marks]

Answer _____

6 (b) Hence find the sum of the squares of all the odd numbers from 1 to 89

[3 marks]

Answer _____

<hr/> 5



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7

$$x^2 - 4x + 7 = 0$$

has roots α and β .

7 (a)

[2 marks]

$$\alpha + \beta = \underline{\hspace{2cm}}$$

$$\alpha\beta = \underline{\hspace{10cm}}$$

7 (b)

[2 marks]

Answer



$$\alpha^4 + \beta^4 = -94$$

$$\alpha^2 + \frac{\beta}{\alpha} \quad \text{and} \quad \beta^2 + \frac{\alpha}{\beta}$$
[illegible]

12

- 8 A hyperbola H_1 has equation

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$$

where a and b are positive constants.

H_1 intersects the x -axis at the points $(6, 0)$ and $(-6, 0)$

The asymptotes of H_1 have equations

$$y = \frac{2}{3}x \quad \text{and} \quad y = -\frac{2}{3}x$$

- 8 (a) Find the values of a and b .

[2 marks]

$a =$ _____

$b =$ _____



8 (b) The hyperbola H_1 is translated by the vector $\begin{bmatrix} 4 \\ 0 \end{bmatrix}$ to give the hyperbola H_2

8 (b) (i) Write down the equation of H_2

[1 mark]

Answer _____

8 (b) (ii) Show that, if the line $y = mx$ intersects H_2 , then the x -coordinates of the points of intersection must satisfy the equation

$$(4 - 9m^2)x^2 - 32x - 80 = 0$$

[3 marks]

Question 8 continues on the next page

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[5 marks]

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11



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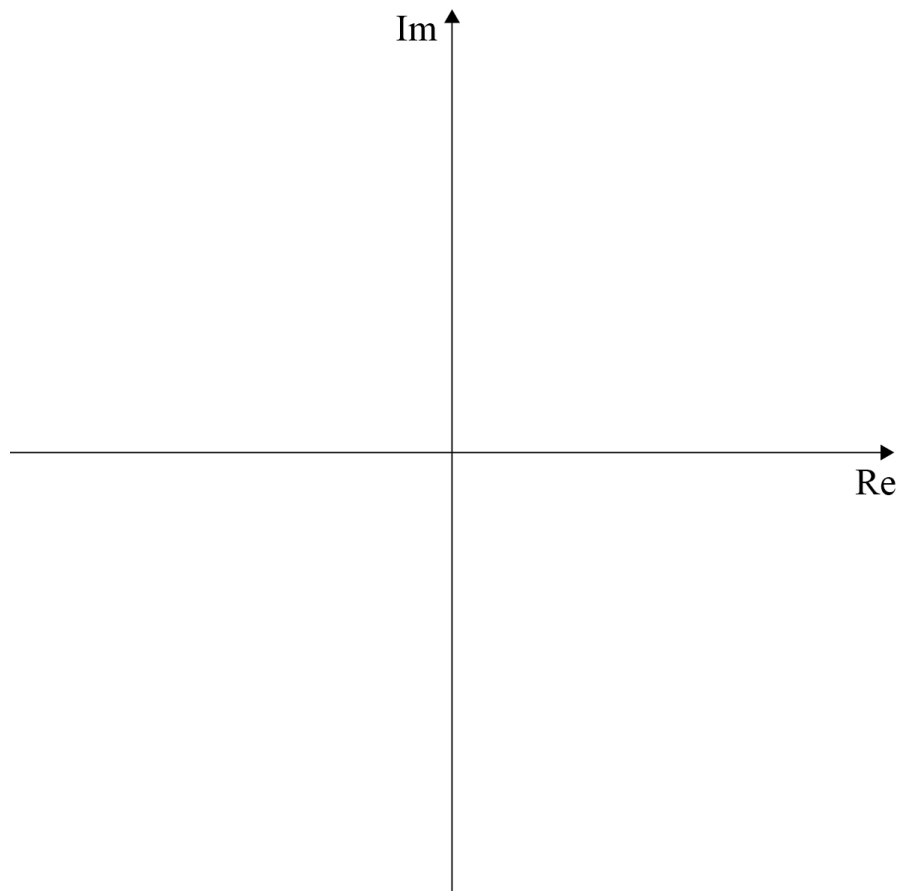
9 The locus L of points satisfies the equation $|z| = |z - 4 - 4i|$

The point P represents the complex number $4 + 4i$

The circle C has centre P and touches L .

9 (a) Sketch L and C on the same Argand diagram in the space below.

[4 marks]



9 (b) Given that z_1 lies on C , find the maximum possible value of $|z_1|$

[3 marks]

Answer _____

9 (c) Given that z_2 lies on C , find the minimum possible value of $\arg(z_2)$

[3 marks]

Answer _____

10

Turn over ►



10 A curve C has the equation

$$y = \frac{(x+5)(x+1)}{x(x-4)}$$

10 (a) State the equations of the asymptotes of C .

[3 marks]

Answer _____



10 (b) (i) Show that

[4 marks]

[illegible]

Turn over ►



No credit will be given for solutions using differentiation.

[illegible]

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